

§ 7.4 #1-4, 10, 11, 13, 14

1. (a) equiangular triangle ( $n=3$ )  $\Rightarrow \frac{360}{3} = 120$   
 (b) " quadrilateral ( $n=4$ )  $\Rightarrow \frac{360}{4} = 90$   
 (c) " octagon ( $n=8$ )  $\Rightarrow \frac{360}{8} = 45$   
 (d) " pentadecagon ( $n=15$ )  $\Rightarrow \frac{360}{15} = 24$   
 (e) " 23-gon ( $n=23$ )  $\Rightarrow \frac{360}{23} = 15\frac{15}{23}$

2. (a) " pentagon ( $n=5$ )  $\Rightarrow \frac{360}{5} = 72 \Rightarrow$  int.  $\angle$  meas.  $= 108$   
 (b) " hexagon ( $n=6$ )  $\Rightarrow \frac{360}{6} = 60 \Rightarrow$  " " "  $= 120$   
 (c) " nonagon ( $n=9$ )  $\Rightarrow \frac{360}{9} = 40 \Rightarrow$  " " "  $= 140$   
 (d) " dodecagon ( $n=12$ )  $\Rightarrow \frac{360}{12} = 30 \Rightarrow$  " " "  $= 120$   
 (e) " 21-gon ( $n=21$ )  $\Rightarrow \frac{360}{21} = 17\frac{1}{7} \Rightarrow$  " " "  $= 172\frac{6}{7}$

3. (a) Each ext.  $\angle = 60^\circ \Rightarrow \frac{360}{n} = 60 \Rightarrow n = 6$  (hexagon)  
 (b) " " "  $= 40^\circ \Rightarrow \frac{360}{n} = 40 \Rightarrow n = 9$  (nonagon)  
 (c) " " "  $= 36^\circ \Rightarrow \frac{360}{n} = 36 \Rightarrow n = 10$  (decagon)  
 (d) " " "  $= 2^\circ \Rightarrow \frac{360}{n} = 2 \Rightarrow n = 180$  (180-gon)  
 (e) " " "  $= 7.5^\circ \Rightarrow \frac{360}{n} = 7.5 \Rightarrow n =$

4. (a) Each  $\angle = 144^\circ \Rightarrow$  each ext.  $\angle = 36^\circ \Rightarrow \frac{360}{n} = 36 \Rightarrow n = 10$  (decagon)  
 (b) " "  $= 120^\circ \Rightarrow$  " " "  $= 60^\circ \Rightarrow \frac{360}{n} = 60 \Rightarrow n = 6$  (hexagon)  
 (c) " "  $= 156^\circ \Rightarrow$  " " "  $= 24^\circ \Rightarrow \frac{360}{n} = 24 \Rightarrow n = 15$  (15-gon)  
 (d) " "  $= 162^\circ \Rightarrow$  " " "  $= 18^\circ \Rightarrow \frac{360}{n} = 18 \Rightarrow n = 20$  (20-gon)  
 (e) " "  $= 172.8^\circ \Rightarrow$  " " "  $= 7.2^\circ \Rightarrow \frac{360}{n} = 7.2 \Rightarrow n = 50$  (50-gon)

10. Sum of measures  $= 5040 \Rightarrow (n-2)180 = 5040$   
 $(n-2) = \frac{5040}{180}$   
 $(n-2) = 28$

$n = 30$

With a 30-gon, each ext.  $\angle$  has measure  $\frac{360}{30} = 12$ .

$\therefore$  each angle measure of the 30-gon  $= 180 - 12 = 168$

11. Let  $x = \text{meas. of one ext. } \angle = \frac{360}{n}$   
 $n = \# \text{ of sides of unknown polygon}$

$180 - x = \text{meas. of one int. } \angle = 180 - \frac{360}{n}$

Note: Each ext.  $\angle$  of a regular hexagon is  $60^\circ$ , from #2(b).  
 Given: sum of int.  $\angle$  measures =  $9(60)$

$$(n-2)180 = 9(60)$$

$$(n-2)180 = 540$$

$$180n - 360 = 540$$

$$180n = 900$$

$$n = 5 \quad (\text{pentagon})$$

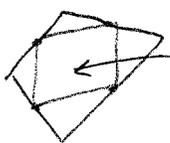
13. (a) Compare  $\frac{360}{n}$  to  $\frac{360}{(2n)}$ . Exterior  $\angle$  measures are indeed halved. Answer: (A)

(b) The word "regular" was omitted. Some decagon ext.  $\angle$ s are large, some small; the same is true of quadrilaterals. Answer: (S)

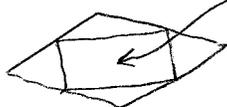
(c) Reg. polygon is both equilat. and equiangular, by def. Answer: (A)

(d) Equilat. polygon may or may not be reg. Answer: (S)



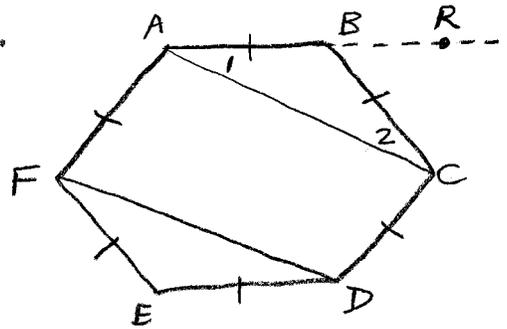
(e)  Parallelogram (could be a rhombus under certain conditions)

Answer: (S)

(f)  Always a rectangle. Answer: (N)

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14. Given:  $ABCDEF$  is a reg. hex.  
Prove:  $ACDF$  is a rect.



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|--|---|
| 1. $ABCDEF$ is a reg. hex.                               | 1. G  |
| 2. $AB=BC=CD=DE=EF=FA$                                   | 2. Def. reg. poly.  |
| 3. Extend $\overleftrightarrow{AB}$ through $R$ as shown | 3. Postulate of Euclidean geometry: Any line can be extended.   |
| 4. $m\angle RBC = \frac{360}{6}$                         | 4. Ext. $\angle$ of a reg. poly.                                |
| 5. $m\angle ABC = 120$                                   | 5. Def. supp.   |
| 6. $m\angle E = 120$                                     | 6. Def. reg. poly. (equiangular)                                |
| 7. $\angle 1 \cong \angle 2$                             | 7. ITT ( $\triangle \Rightarrow \triangle$ )                    |
| 8. $m\angle 1 + m\angle 2 + m\angle ABC = 180$           | 8. Angles of $\triangle$ add to $180^\circ$                     |
| 9. $m\angle 1 = m\angle 2 = 30$                          | 9. Alg. (steps obvious from (7) and (8), omitted to save space) |
| 10. $m\angle FAB = 120$                                  | 10. Def. equiang., see also (5,6)                               |
| 11. $m\angle FAC = 90$                                   | 11. Subtr.  |
| 12. $\triangle ABC \cong \triangle DEF$                  | 12. SAS (2, 5, 6, 2)  |
| 13. $\overline{AC} \cong \overline{DF}$                  | 13. CPCTC   |
| 14. $ACDF$ is a $\square$                                | 14. Both prs. opp. sides $\cong$ (13, 2)                        |
| 15. $ACDF$ is a rect.                                    | 15. $\square$ with a rt. $\angle$ (14, 11)                      |

□