

## Test on Vec/Trig/Prob/Stat

**Instructions:** Graphing calculator and PENCIL are required. If you need more room for rough scratch work, use the reverse sides, which will not be graded (unless you need more room for work that is to be graded, in which case you should write OVER and continue on the back side). Circle all answers in problems involving work (no need to circle if the answer is a fill-in without any work).

**Note:** Round all approximate answers to 4 decimal places after the decimal point unless otherwise stated.

### Part I: Short Answer (4 pts. each, except for the first one, which is scored pass-fail)

1. If the answer to a probability or expected-value question (e.g., the expected number of people who will be able to board an aircraft within the first 5 minutes of boarding) is *really* important in the world of business, how should you go about finding an answer? \_\_\_\_\_  
\_\_\_\_\_
- 2,3. There are 79 students in Form IV. On a certain day, there is a fire drill, and 60 of the Form IV students (randomly chosen from the entire form) find themselves on Grant Meadow, attempting to line up in a single-file line. Because only a few of them are good at alphabetizing themselves, they arrange themselves in a randomly-ordered single-file line. In how many different ways can the 79 students of Form IV be arranged in a single-file line of 60 people? Order matters, obviously. Give both an exact answer (using appropriate symbols) and an approximate answer (to the nearest power of 10).  
Exact (symbolic): \_\_\_\_\_ Approximate answer: 10 to the \_\_\_\_\_ power
4. The law of sines can sometimes run into a problem with ambiguous cases. The ambiguous case can occur whenever there is a possibility that the unknown angle is the \_\_\_\_\_ of the three angles in the triangle.
- 5,6. If the unknown angle in a triangle has a sine of 0.616, then the angle could be either \_\_\_\_\_ or \_\_\_\_\_ (give answers to the nearest tenth of a degree).
7. At a large university, 61% of the students like Bernie Sanders, 51% like Hillary Clinton, and 40% like both candidates. The probability that a randomly selected student likes at least one of these two candidates is \_\_\_\_\_. (**Warning: Instant failure if you say 112%.**)
8. Let  $\mathbf{u} = \langle 4, 6 \rangle$ , and let  $\mathbf{v} = \langle -1.5, 6 \rangle$ . Find the magnitude of the vector that connects the terminal point of vector  $\mathbf{u}$  to the terminal point of vector  $\mathbf{v}$ . No work is required. Answer: \_\_\_\_\_
9. The other word we used for magnitude (of a vector) is \_\_\_\_\_.
- 10,11. Two vectors (neither of which is  $\langle 0, 0 \rangle$ ) are said to be *perpendicular* (or *orthogonal*) if and only if their dot product is zero. Compute the dot product:  $\langle 8, -2 \rangle \cdot \langle -3, -12 \rangle =$  \_\_\_\_\_.  
Are these two vectors perpendicular? \_\_\_\_\_
12. Find the area of a triangle whose sides have lengths 24 ft., 32 ft., and 40 ft. Work is optional, but be sure to circle your answer.

**Part II. Free Response (12 pts. per numbered problem). Work is required for full credit. Give all approximate answers in a decimal format, rounded to 4 decimal places after the decimal point.**

13. An urn contains 16 identically sized balls, 8 of which are black and 8 of which are red. Those are the only balls present in the urn.
- (a) Compute the probability of obtaining two reds and a black (in that order) when balls are drawn randomly, without replacement.
  - (b) Compute the probability of obtaining at least one red ball when 3 balls are drawn randomly, without replacement.
  - (c) Compute the probability of obtaining two reds and a green (in that order) when balls are drawn randomly, *with* replacement.
14. Three cards are drawn, without replacement, from a standard 52-card deck that has been shuffled well.
- (a) Compute the probability of obtaining 3 aces.
  - (b) Compute the probability of obtaining at least one ace.
  - (c) Compute the probability of obtaining 2 aces and 1 king (in any order).

15. Below, make a reasonably neat sketch of triangle ABC that has the following given information:  $a = 11$ ,  $b = 11$ ,  $\angle C = 22^\circ$ . (Angle C is what your textbook commonly called  $\gamma$ .) Then solve the triangle. Put rough sketch work on the back of one of the other sheets. What you show below should be clean and coherent. Sides must be correct to 4 decimal places after the decimal point, and angles should be given in the format  $xx^\circ xx.x'$ , where the  $'$  symbol denotes minutes.

16. Sketch vectors  $\mathbf{u} = \langle 3, -5 \rangle$ ,  $\mathbf{v} = \langle -4, 8 \rangle$ , and the vector  $\mathbf{u} + \mathbf{v}$ , all on the same set of axes. (Make your sketch down below, after the questions. Make your sketch medium-sized, so that your middle-aged teacher with his weak eyes will be able to grade it.)

(a) Label each vector.

(b) Compute the vector  $2\mathbf{u} - 3\mathbf{v}$ . No need to sketch it, but for full credit you must begin by writing  $2\mathbf{u} - 3\mathbf{v} = \dots$ . Remember to circle your answer. Show enough work so that it is clear that you know what you are doing.

(c) Write two correct notations for the zero vector. (The zero vector is the vector that, when added to another vector, does not change it.)

Notation 1: \_\_\_\_\_ Notation 2: \_\_\_\_\_

17. Solve the triangle whose sides have lengths 14 m, 8 m, and 12 m, and find the area to the nearest tenth of a square meter. Give angles to the nearest tenth of a degree. A sketch is required.