

$$\frac{-350(N+1)}{-2N} = x^2$$

MH
p.3

$$x^2 = 175 \cdot \frac{N+1}{N}$$

$$x_{\text{crit}} = \pm \sqrt{175 \cdot \frac{N+1}{N}}, \text{ discard neg. root}$$

Must verify that this gives a min.!

Easiest way is by 2nd deriv. test:

$$W''(x) = 0 + 700(N+1)x^{-3} > 0 \text{ since } x > 0$$

Since W'' is positive for any x in the domain,

$$W''(x_{\text{crit}}) > 0 \text{ also.}$$

$\therefore x_{\text{crit}}$ gives a local min., and since there are no other crit. pts. or endpts., x_{crit} gives a global min. as well

$$\text{When } N=6, x_{\text{crit}} = \sqrt{175 \cdot \frac{7}{6}} \approx 14.289$$

$$y = \frac{350}{x_{\text{crit}}} = \frac{350}{\sqrt{175 \cdot \frac{7}{6}}} \approx 24.495$$

14.289 ft by 24.495 ft, the latter being the common wall

$$(b) \text{ When } N=10, x_{\text{crit}} = \sqrt{175 \cdot \frac{11}{10}} \approx 13.874$$

$$y = \frac{350}{\sqrt{175 \cdot \frac{11}{10}}} \approx 25.226$$

13.874 ft by 25.226 ft, " " " " " "

$$\text{When } N=3, x_{\text{crit}} = \sqrt{175 \cdot \frac{4}{3}} \approx 15.275$$

$$y = \frac{350}{\sqrt{175 \cdot \frac{4}{3}}} \approx 22.913$$

15.275 ft by 22.913 ft, " " " " " "

Question: How much explanation is needed in these optimization problems?

Answer: About as much as is shown here, minus the square-bracketed comments. You need to demonstrate knowledge of the calculus. Reasoning from a graph alone is not allowed on free-response AP problems.